

Розрахункова робота № 1

Тема. Інтеграли. Застосування інтегралів.

Завдання 1. Обчислити інтеграли.

1.1. $\int \frac{3+\sqrt[3]{x^2}-2x}{\sqrt{x}} dx.$

1.2. $\int \frac{2x^2+3\sqrt{x}-1}{2x} dx.$

1.3. $\int \frac{3\sqrt{x}+4x^2-5}{2x} dx.$

1.4. $\int \frac{2\sqrt{x}-x^2+3}{\sqrt[3]{x}} dx.$

1.5. $\int \frac{\sqrt[4]{x}-2x+5}{x^2} dx.$

1.6. $\int \frac{2x^3-\sqrt{x}+4}{\sqrt{x}} dx.$

1.7. $\int (\sqrt[3]{x}-\frac{2\sqrt[4]{x}}{x}+3) dx.$

1.8. $\int \frac{2x^3-\sqrt{x^5}+1}{\sqrt{x}} dx.$

1.9. $\int \frac{3x^2-\sqrt[5]{x}+2}{x} dx.$

1.10. $\int \frac{2x^3-\sqrt{x}+4}{x^2} dx.$

1.11. $\int \frac{\sqrt[6]{x^5}-5x^2+3}{x} dx.$

1.12. $\int (x\sqrt{x}-\frac{1}{\sqrt{x^3}}+1) dx.$

1.13. $\int (x^2-\frac{\sqrt{x}}{x}-3) dx.$

1.14. $\int \frac{\sqrt[3]{x^2}-2x^5+3}{x} dx.$

1.15. $\int (\frac{\sqrt[3]{x}}{x}+2x^3-4) dx.$

1.16. $\int \frac{\sqrt{x^3}-3x^4+2}{x} dx.$

1.17. $\int (2x^3-3\sqrt{x^5}+\frac{4}{x}) dx.$

1.18. $\int \frac{2x^3-\sqrt{x^5}+5}{x^2} dx.$

1.19. $\int \frac{3x^2-\sqrt{x^2}+7}{x^2} dx.$

1.20. $\int \frac{3x^4-\sqrt[3]{x^2}+1}{x^2} dx.$

1.21. $\int (\sqrt[5]{x^2}-\frac{2}{x^3}+4) dx.$

1.22. $\int \frac{\sqrt{x}-2x^3+6}{x} dx.$

1.23. $\int \frac{\sqrt[5]{x}-2x^3+4}{x^2} dx.$

1.24. $\int (\sqrt{x}-\frac{3x^2}{\sqrt{x^3}}+2) dx.$

1.25. $\int (\sqrt[5]{x}-\frac{4}{x^5}+2) dx.$

1.26. $\int \frac{\sqrt[7]{x^6}-2x^2+3}{x} dx.$

1.27. $\int (\frac{\sqrt[3]{x}}{x}-\frac{2}{x^3}+1) dx.$

1.28. $\int (\frac{2x^2}{\sqrt{x}}-\frac{5}{x}+6) dx.$

$$1.29. \int \left(\frac{\sqrt[3]{x^2}}{x} - \frac{7}{x^3} + 5 \right) dx.$$

$$1.30. \int \left(\frac{5x^2}{\sqrt{x}} - \sqrt[3]{x^2} + 2 \right) dx.$$

Завдання 2. Обчислити інтеграли.

$$2.1. \int \sqrt{3+x} dx.$$

$$2.2. \int \sqrt[3]{1+x} dx.$$

$$2.3. \int \sqrt[3]{(1+x)^2} dx.$$

$$2.4. \int \frac{dx}{\sqrt{1+x}}.$$

$$2.5. \int \frac{dx}{\sqrt{(1-x)^3}}.$$

$$2.6. \int \frac{dx}{\sqrt[3]{2+x}}.$$

$$2.7. \int (1-4x)^7 dx.$$

$$2.8. \int (1+4x)^5 dx.$$

$$2.9. \int (1-3x)^4 dx.$$

$$2.10. \int \sqrt{1+3x} dx.$$

$$2.11. \int \sqrt{5-4x} dx.$$

$$2.12. \int \frac{dx}{\sqrt[3]{5+3x}}.$$

$$2.13. \int \frac{dx}{\sqrt[3]{(1-4x)^5}}.$$

$$2.14. \int \frac{dx}{\sqrt[3]{(3-4x)^2}}.$$

$$2.15. \int \frac{dx}{\sqrt[3]{2-5x}}.$$

$$2.16. \int \sqrt[5]{3-2x} dx.$$

$$2.17. \int \sqrt[4]{1+3x} dx.$$

$$2.18. \int \sqrt[3]{1+3x} dx.$$

$$2.19. \int \frac{dx}{\sqrt{(3-x)^5}}.$$

$$2.20. \int \frac{dx}{\sqrt[3]{3+x}}.$$

$$2.21. \int \frac{dx}{(2+x)^3}.$$

$$2.22. \int \sqrt[3]{5-2x} dx.$$

$$2.23. \int \sqrt{5-4x} dx.$$

$$2.24. \int \sqrt[5]{(6-5x)^2} dx.$$

$$2.25. \int \sqrt[4]{2-5x} dx.$$

$$2.26. \int \sqrt[3]{4-2x} dx.$$

$$2.27. \int \sqrt{3-4x} dx.$$

$$2.28. \int \sqrt[5]{3+2x} dx.$$

$$2.29. \int \sqrt[4]{(3+5x)^3} dx.$$

$$2.30. \int \sqrt[3]{(2-x)^2} dx.$$

Завдання 3. Обчислити інтеграли.

$$3.1. \int \frac{\sqrt{3} dx}{9x^2-3}.$$

$$3.2. \int \frac{dx}{\sqrt{9x^2+3}}.$$

- 3.3. $\int \frac{dx}{9x^2 + 3}$.
- 3.5. $\int \frac{dx}{\sqrt{3-9x^2}}$.
- 3.7. $\int \frac{3dx}{\sqrt{7x^2 - 4}}$.
- 3.9. $\int \frac{dx}{5x^2 - 3}$.
- 3.11. $\int \frac{dx}{\sqrt{5x^2 + 3}}$.
- 3.13. $\int \frac{\sqrt{5}dx}{\sqrt{3-4x^2}}$.
- 3.15. $\int \frac{dx}{2x^2 + 7}$.
- 3.17. $\int \frac{xdx}{\sqrt{5-4x^2}}$.
- 3.19. $\int \frac{3xdx}{4x^2 + 1}$.
- 3.21. $\int \frac{dx}{\sqrt{2-5x^2}}$.
- 3.23. $\int \frac{dx}{\sqrt{7x^2 - 3}}$.
- 3.25. $\int \frac{dx}{2x^2 + 3}$.
- 3.27. $\int \frac{dx}{2x^2 + 9}$.
- 3.29. $\int \frac{dx}{\sqrt{9x^2 + 2}}$.
- 3.4. $\int \frac{9dx}{\sqrt{9x^2 - 3}}$.
- 3.6. $\int \frac{dx}{7x^2 - 4}$.
- 3.8. $\int \frac{dx}{5x^2 + 3}$.
- 3.10. $\int \frac{dx}{\sqrt{3-5x^2}}$.
- 3.12. $\int \frac{dx}{\sqrt{4-7x^2}}$.
- 3.14. $\int \frac{dx}{\sqrt{2x^2 - 9}}$.
- 3.16. $\int \frac{dx}{\sqrt{3x^2 + 1}}$.
- 3.18. $\int \frac{xdx}{\sqrt{5-3x^2}}$.
- 3.20. $\int \frac{4xdx}{\sqrt{3-4x^2}}$.
- 3.22. $\int \frac{dx}{2x^2 - 5}$.
- 3.24. $\int \frac{dx}{5x^2 + 2}$.
- 3.26. $\int \frac{dx}{\sqrt{5x^2 + 1}}$.
- 3.28. $\int \frac{dx}{\sqrt{9-2x^2}}$.
- 3.30. $\int \frac{dx}{5x^2 - 4}$.

Завдання 4. Обчислити інтеграли.

- 4.1 $\int \frac{dx}{(2x+1)\sqrt[3]{\ln^2(2x+1)}}$.
- 4.2 $\int \frac{\sqrt[3]{\ln^2(1-x)}}{x-1} dx$.

$$4.3. \int \frac{dx}{(1-x)\sqrt[3]{\ln^2(1-x)}}.$$

$$4.5. \int \frac{\ln^3(1-x)}{x-1} dx.$$

$$4.7. \int \frac{\sqrt[3]{\ln(3x+1)}}{3x+1} dx.$$

$$4.9. \int \frac{dx}{(x+1)\sqrt[3]{\ln(x+1)}}.$$

$$4.11. \int \frac{\sqrt{\ln^5(x+1)}}{x+1} dx.$$

$$4.13. \int \frac{\sqrt{\ln^3(x+1)}}{x+1} dx.$$

$$4.15. \int \frac{dx}{(x+1)\sqrt[5]{\ln(x+1)}}.$$

$$4.17. \int \frac{\sqrt{\ln^3(x+1)}}{x+1} dx.$$

$$4.19. \int \frac{\sqrt{\ln^5(x+1)}}{x+1} dx.$$

$$4.21. \int \frac{dx}{(x+1)\sqrt[3]{\ln(x+1)}}.$$

$$4.23. \int \frac{\sqrt{\ln^3(x+3)}}{x+3} dx.$$

$$4.25. \int \frac{\sqrt{\ln^5(x+3)}}{x+3} dx.$$

$$4.27. \int \frac{\ln(3x+5)}{3x+5} dx.$$

$$4.29. \int \frac{\ln^6(x+9)}{x+9} dx.$$

$$4.4. \int \frac{dx}{(1-x)\sqrt{\ln^3(1-x)}}.$$

$$4.6. \int \frac{\sqrt{\ln(2x-1)}}{2x-1} dx.$$

$$4.8. \int \frac{dx}{(x+1)\ln^2(x+1)}.$$

$$4.10. \int \frac{dx}{(x+1)\ln^2(x+1)}.$$

$$4.12. \int \frac{\sqrt[7]{\ln^2(x+1)}}{x+1} dx.$$

$$4.14. \int \frac{dx}{(x+1)\sqrt[5]{\ln(x+1)}}.$$

$$4.16. \int \frac{dx}{(x+2)\sqrt{\ln(x+2)}}.$$

$$4.18. \int \frac{dx}{(x-3)\ln^4(x-3)}.$$

$$4.20. \int \frac{\ln^3(x-5)}{x-5} dx.$$

$$4.22. \int \frac{dx}{(x-3)\ln^4(x-3)}.$$

$$4.24. \int \frac{\sqrt[3]{\ln^4(x-5)}}{x-5} dx.$$

$$4.26. \int \frac{\ln^5(x-8)}{x-8} dx.$$

$$4.28. \int \frac{dx}{(x-4)\ln^5(x-4)}.$$

$$4.30. \int \frac{\ln(3x+5)}{3x+5} dx.$$

Завдання 5. Обчислити інтеграли.

$$5.1. \int \frac{\sqrt{\arctg^6 3x}}{1+9x^2} dx.$$

$$5.2. \int \frac{\sqrt[3]{\arcsin x}}{\sqrt{1-x^2}} dx.$$

$$5.3. \int \frac{\arccos^2 3x}{\sqrt{1-9x^2}} dx .$$

$$5.5. \int \frac{\sqrt[3]{\arccos^2 x}}{\sqrt{1-x^2}} dx .$$

$$5.7. \int \frac{\arccos^3 2x}{\sqrt{1-4x^2}} dx .$$

$$5.9. \int \frac{\arcsin^5 2x}{\sqrt{1-4x^2}} dx .$$

$$5.11. \int \frac{\arccos^3 2x}{\sqrt{1-4x^2}} dx .$$

$$5.13. \int \frac{\arccos 4x}{\sqrt{1-16x^2}} dx .$$

$$5.15. \int \frac{\arcsin^3 2x}{\sqrt{1-4x^2}} dx .$$

$$5.17. \int \frac{\sqrt[3]{\operatorname{arctg} 2x}}{1+4x^2} dx .$$

$$5.19. \int \frac{\sqrt{\operatorname{arctg}^3 x}}{1+x^2} dx .$$

$$5.21. \int \frac{dx}{(1+x^2) \operatorname{arctg}^5 x} .$$

$$5.23. \int \frac{\sqrt[3]{\arccos 2x}}{\sqrt{1-4x^2}} dx .$$

$$5.25. \int \frac{\arcsin^2 5x}{\sqrt{1-25x^2}} dx .$$

$$5.27. \int \frac{\operatorname{arctg}^8 3x}{1+9x^2} dx .$$

$$5.29. \int \frac{\sqrt[5]{\operatorname{arctg}^3 x}}{1+x^2} dx .$$

$$5.4. \int \frac{\operatorname{arctg}^3 2x}{1+4x^2} dx .$$

$$5.6. \int \frac{dx}{(1+x^2) \operatorname{arctg}^3 x} .$$

$$5.8. \int \frac{\sqrt[3]{\operatorname{arctg}^2 x}}{1+x^2} dx .$$

$$5.10. \int \frac{dx}{\sqrt{1-x^2} \arcsin^4 x} .$$

$$5.12. \int \frac{\operatorname{arctg}^7 3x}{1+9x^2} dx .$$

$$5.14. \int \frac{\arcsin^4 x}{\sqrt{1-x^2}} dx .$$

$$5.16. \int \frac{dx}{(1+x^2) \operatorname{arctg}^7 x} .$$

$$5.18. \int \frac{\arccos^6 3x}{\sqrt{1-9x^2}} dx .$$

$$5.20. \int \frac{dx}{(1+x^2) \sqrt{\operatorname{arctg} x}} .$$

$$5.22. \int \frac{\arccos^7 x dx}{\sqrt{1-x^2}} .$$

$$5.24. \int \frac{\operatorname{arctg}^4 5x}{1+25x^2} dx .$$

$$5.26. \int \frac{dx}{\sqrt{1-25x^2} \arcsin 5x} .$$

$$5.28. \int \frac{\arccos^2 7x}{\sqrt{1-49x^2}} dx .$$

$$5.30. \int \frac{\operatorname{arctg}^4 8x}{1+64x^2} dx .$$

Завдання 6. Обчислити інтеграли.

6.1. $\int \frac{dx}{4x^2 - 5x + 4}.$

6.3. $\int \frac{dx}{2x^2 - 7x + 1}.$

6.5. $\int \frac{dx}{5x^2 + 2x + 7}.$

6.7. $\int \frac{dx}{2x^2 - 11x + 2}.$

6.9. $\int \frac{dx}{3x^2 - 12x + 3}.$

6.11. $\int \frac{dx}{x^2 - 5x + 6}.$

6.13. $\int \frac{dx}{3x^2 - 8x - 3}.$

6.15. $\int \frac{dx}{5x - x^2 - 6}.$

6.17. $\int \frac{dx}{\sqrt{3x^2 - 4x + 1}}.$

6.19. $\int \frac{dx}{\sqrt{x^2 + 6x + 8}}.$

6.21. $\int \frac{dx}{\sqrt{3 + 2x - 2x^2}}.$

6.23. $\int \frac{dx}{\sqrt{1 + x - x^2}}.$

6.25. $\int \frac{dx}{\sqrt{2x + 3 - x^2}}.$

6.27. $\int \frac{dx}{\sqrt{1 + 2x - x^2}}.$

6.29. $\int \frac{dx}{\sqrt{2 + 4x - 3x^2}}.$

6.2. $\int \frac{dx}{x^2 - 4x + 10}.$

6.4. $\int \frac{dx}{2x^2 + x - 6}.$

6.6. $\int \frac{dx}{2x^2 - 2x + 1}.$

6.8. $\int \frac{dx}{2x^2 + x + 2}.$

6.10. $\int \frac{dx}{2x^2 + 3x + 2}.$

6.12. $\int \frac{dx}{2x - 3 - 4x^2}.$

6.14. $\int \frac{dx}{8 - 2x - x^2}.$

6.16. $\int \frac{dx}{\sqrt{4 + 8x - x^2}}.$

6.18. $\int \frac{dx}{\sqrt{2 - 3x - 2x^2}}.$

6.20. $\int \frac{dx}{\sqrt{2 + 8x - 2x^2}}.$

6.22. $\int \frac{dx}{2 - 2x - 3x^2}.$

6.24. $\int \frac{dx}{\sqrt{5x^2 - 10x + 4}}.$

6.26. $\int \frac{dx}{4x^2 - 8x + 3}.$

6.28. $\int \frac{dx}{\sqrt{4x^2 - x + 4}}.$

6.30. $\int \frac{dx}{4x^2 + 2x + 4}.$

Завдання 7. Обчислити інтеграли.

7.1. $\int \frac{x+1}{2x^2 + 3x - 4} dx.$

7.2. $\int \frac{x+6}{3x^2 + x + 1} dx.$

7.3. $\int \frac{2x-1}{3x^2-2x+6} dx.$

7.5. $\int \frac{x+5}{x^2+x-2} dx.$

7.7. $\int \frac{x+4}{2x^2-6x-8} dx.$

7.9. $\int \frac{5x-2}{2x^2-5x+2} dx.$

7.11. $\int \frac{x+1}{2x^2+x+1} dx.$

7.13. $\int \frac{4x+8}{4x^2+6x-13} dx.$

7.15. $\int \frac{xdx}{2x^2+2x+5} dx.$

7.17. $\int \frac{x-3}{\sqrt{2x^2-4x-1}} dx.$

7.19. $\int \frac{2x+1}{\sqrt{1+x-3x^2}} dx.$

7.21. $\int \frac{2x-10}{\sqrt{1+x-x^2}} dx.$

7.23. $\int \frac{3x+4}{\sqrt{x^2+6x+13}} dx.$

7.25. $\int \frac{5x+2}{\sqrt{x^2+3x-4}} dx.$

7.27. $\int \frac{2x-1}{\sqrt{x^2-3x+4}} dx.$

7.29. $\int \frac{5x-3}{\sqrt{2x^2+4x-5}} dx.$

7.4. $\int \frac{xdx}{2x^2+x+5} dx.$

7.6. $\int \frac{3x-2}{5x^2-3x+2} dx.$

7.8. $\int \frac{x+4}{2x^2-7x+1} dx.$

7.10. $\int \frac{4x-1}{4x^2-4x+5} dx.$

7.12. $\int \frac{x+1}{3x^2-2x-3} dx.$

7.14. $\int \frac{5x+1}{x^2-4x+1} dx.$

7.16. $\int \frac{2x-13}{\sqrt{3x^2-3x-16}} dx.$

7.18. $\int \frac{x-1}{\sqrt{3x^2-x+5}} dx.$

7.20. $\int \frac{2x+5}{\sqrt{4x^2+8x+9}} dx.$

7.22. $\int \frac{2x-8}{\sqrt{1-x+x^2}} dx.$

7.24. $\int \frac{3x-1}{\sqrt{2x^2-5x+1}} dx.$

7.26. $\int \frac{x-4}{\sqrt{2x^2-x+7}} dx.$

7.28. $\int \frac{4x+1}{\sqrt{2+x-x^2}} dx.$

7.30. $\int \frac{3x+2}{\sqrt{4+2x-x^2}} dx.$

Завдання 9. Обчислити інтеграли.

9.1. $\int (x-7) \cos 2x dx.$

9.3. $\int (x-5) \cos x dx.$

9.2. $\int (x-4) \sin 2x dx.$

9.4. $\int (x-4) \cos 2x dx.$

9.5. $\int (x+8) \sin 3x dx$.

9.7. $\int (x+4) \cos \frac{x}{2} dx$.

9.9. $\int \ln(x-5) dx$.

9.11. $\int x^2 e^{-x} dx$.

9.13. $\int \arcsin 5x dx$.

9.15. $\int x^2 e^{3x} dx$.

9.17. $\int \arcsin 2x dx$.

9.19. $\int x e^{-4x} dx$.

9.21. $\int x \sin(x-2) dx$.

9.23. $\int x \sin(x-5) dx$.

9.25. $\int \arctg \frac{x}{2} dx$.

9.27. $\int \ln(2x-1) dx$.

9.29. $\int \arctg \frac{x}{4} dx$.

9.6. $\int (x+2) \sin \frac{x}{2} dx$.

9.8. $\int (x-9) \sin \frac{x}{2} dx$.

9.10. $\int \arctg 2x dx$.

9.12. $\int \arctg 4x dx$.

9.14. $\int x \arctg x dx$.

9.16. $\int x \cos(x+4) dx$.

9.18. $\int (x^2-3) e^x dx$.

9.20. $\int \arcsin 3x dx$.

9.22. $\int x \cos(x+4) dx$.

9.24. $\int x \cos(x+6) dx$.

9.26. $\int \ln(x+8) dx$.

9.28. $\int \arccos \frac{x}{5} dx$.

9.30. $\int \arccos \frac{x}{3} dx$.

Завдання 11. Обчислити інтеграли.

11.1. $\int \frac{dx}{2+\sqrt{x+3}}$.

11.3. $\int \frac{x^2 dx}{\sqrt{x-3}}$.

11.5. $\int \frac{x^3 dx}{\sqrt{x+1}}$.

11.7. $\int \frac{dx}{(x+1)\sqrt{x+4}}$.

11.9. $\int \frac{dx}{\sqrt{x+3}}$.

11.11. $\int \frac{1+x}{x+\sqrt{x}} dx$.

11.2. $\int \frac{xdx}{\sqrt{x+3}}$.

11.4. $\int \frac{xdx}{2+\sqrt{x+4}}$.

11.6. $\int \frac{x+1}{x\sqrt{x+2}} dx$.

11.8. $\int \frac{\sqrt{x+2}}{x-3} dx$.

11.10. $\int \frac{dx}{\sqrt{x(x+3)}}$.

11.12. $\int \frac{xdx}{\sqrt{x-1}}$.

$$11.13. \int \frac{\sqrt{x} dx}{x-1}.$$

$$11.15. \int \frac{dx}{1+\sqrt{x-1}}.$$

$$11.17. \int \frac{x+1}{x\sqrt{x-1}} dx.$$

$$11.19. \int \frac{x^2 dx}{\sqrt{x-4}}.$$

$$11.21. \int \frac{x^3 dx}{\sqrt{x+2}}.$$

$$11.23. \int \frac{dx}{\sqrt{x}(x-1)}.$$

$$11.25. \int \frac{dx}{x\sqrt{x-2}}.$$

$$11.27. \int \frac{x-1}{x\sqrt{x-2}} dx.$$

$$11.29. \int \frac{dx}{3+\sqrt{x-6}}.$$

$$11.14. \int \frac{dx}{3+\sqrt{x+5}}.$$

$$11.16. \int \frac{dx}{x\sqrt{x-7}}.$$

$$11.18. \int \frac{x^3 dx}{\sqrt{x-7}}.$$

$$11.20. \int \frac{\sqrt{x+4}}{x} dx.$$

$$11.22. \int \frac{\sqrt{x} dx}{x+10}.$$

$$11.24. \int \frac{dx}{1+\sqrt{x-2}}.$$

$$11.26. \int \frac{x^2 dx}{\sqrt{x-2}}.$$

$$11.28. \int \frac{x^3 dx}{\sqrt{x+6}}.$$

$$11.30. \int \frac{dx}{2+\sqrt{x-8}}.$$

Завдання 13. Обчислити інтеграли.

$$13.1. \int \cos^4 3x \sin^2 3x dx.$$

$$13.3. \int \cos^3 x \sin^8 x dx.$$

$$13.5. \int \frac{\cos^3 x dx}{\sqrt[3]{\sin^4 x}}.$$

$$13.7. \int \frac{\cos^3 x}{\sqrt[3]{\sin^2 x}} dx.$$

$$13.9. \int \frac{3 \sin^3 x}{\cos^4 x} dx.$$

$$13.11. \int \frac{\sin^3 x}{\sqrt[5]{\cos^3 x}} dx.$$

$$13.13. \int \sqrt[3]{\sin^2 x \cos^3 x} dx.$$

$$13.2. \int \sqrt[5]{\sin^4 x \cos^3 3x} dx.$$

$$13.4. \int \cos^4 x \sin^3 x dx.$$

$$13.6. \int \sqrt[5]{\sin^3 2x \cos^3 2x} dx.$$

$$13.8. \int \frac{\sin^3 x}{\sqrt[3]{\cos^4 x}} dx.$$

$$13.10. \int \sin^5 x \cos^4 x dx.$$

$$13.12. \int \sqrt[3]{\cos^2 x \sin^3 x} dx.$$

$$13.14. \int \sqrt[5]{\cos^3 2x \sin^3 2x} dx.$$

$$13.15. \int \frac{\cos^3 x dx}{\sqrt[3]{\sin^3 x}}$$

$$13.17. \int \frac{\sin^3 x}{\sqrt[3]{\cos^2 x}} dx$$

$$13.19. \int \sin^4 2x \cos^2 2x dx$$

$$13.21. \int \frac{\sin^3 2x}{\sqrt[3]{\cos^2 2x}} dx$$

$$13.23. \int \sin^2 x \cos^4 x dx$$

$$13.25. \int \sin^3 x \cos^8 x dx$$

$$13.27. \int \sin^5 x \sqrt{\cos^3 x} dx$$

$$13.29. \int \sin^4 3x \cos^2 3x dx$$

$$13.16. \int \sin^2 2x \cos^4 2x dx$$

$$13.18. \int \sqrt[5]{\cos^4 x} \sin^3 x dx$$

$$13.20. \int \frac{\cos^3 2x}{\sqrt[3]{\sin^2 2x}} dx$$

$$13.22. \int \sin^4 x \cos^3 x dx$$

$$13.24. \int \sin^4 x \cos^2 x dx$$

$$13.26. \int \frac{3 \cos^3 x}{\sin^4 x} dx$$

$$13.28. \int \sin^4 x \cos^5 x dx$$

$$13.30. \int \frac{\sin^3 x}{\sqrt[3]{\cos^4 x}} dx$$

Завдання 14. Користуючись

формулою Ньютона-Лейбніца,

обчислити інтеграли.

$$14.1. \int_0^{\sqrt{3}} x \sqrt[3]{1+x^2} dx$$

$$14.3. \int_0^1 \frac{x^2 dx}{x^2+1}$$

$$14.5. \int_0^{\pi/2} \frac{\cos x}{1+\cos x} dx$$

$$14.7. \int_0^{-3} \frac{dx}{\sqrt{25+3x}}$$

$$14.9. \int_1^e \frac{1+\ln x}{x} dx$$

$$14.11. \int_{\pi/4}^{\pi/2} \frac{dx}{1-\cos^2 x}$$

$$14.13. \int_0^1 x^3 \sqrt{4+5x^4} dx$$

$$14.2. \int_0^{12\sqrt{3}} \frac{12x^5 dx}{\sqrt{x^6+1}}$$

$$14.4. \int_0^{\pi/2} \sin x \cos^2 x dx$$

$$14.6. \int_{3/4}^{4/3} \frac{dx}{x^2+1}$$

$$14.8. \int_0^2 \frac{x^3 dx}{\sqrt{x^4+4}}$$

$$14.10. \int_0^1 \frac{x^3}{x^8+1} dx$$

$$14.12. \int_2^5 \frac{dx}{\sqrt{5+4x-x^2}}$$

$$14.14. \int_{-\pi}^{\pi} \sin^2 \frac{x}{2} dx$$

$$14.15. \int_1^2 \frac{e^{1/x}}{x^2} dx.$$

$$14.17. \int_0^1 3(x^2 + x^2 e^{x^3}) dx.$$

$$14.19. \int_1^{\sqrt{3}} \frac{x^2 dx}{1+x^6}.$$

$$14.21. \int_1^{\sqrt{e}} \frac{dx}{x\sqrt{1-\ln^2 x}}.$$

$$14.23. \int_{\pi/6}^{\pi/2} \sin x \cos^3 x dx.$$

$$14.25. \int_0^1 \frac{dx}{\sqrt{4-3x}}.$$

$$14.27. \int_1^e \frac{\ln^2 x}{x} dx.$$

$$14.29. \int_{\pi/6}^{\pi/2} \cos \alpha \sin^3 \alpha d\alpha.$$

$$14.16. \int_0^{1/2} \frac{xdx}{\sqrt{1-x^2}}.$$

$$14.18. \int_{\pi^2/9}^{\pi^2} \frac{\cos \sqrt{x}}{\sqrt{x}} dx.$$

$$14.20. \int_1^e \frac{\sin \ln x}{x} dx.$$

$$14.22. \int_3^8 \sqrt{x+1} dx.$$

$$14.24. \int_{\pi/18}^{\pi/6} 12 \operatorname{ctg} 3xdx.$$

$$14.26. \int_1^{\sqrt{2}} \frac{xdx}{\sqrt{4-x^2}}.$$

$$14.28. \int_{-1}^0 \frac{dx}{4x^2-9}.$$

$$14.30. \int_0^{\sqrt{\pi}/4} \frac{xdx}{\cos^2(x^2)}.$$

Завдання 15. Обчислити невідкладні інтеграли або довести їх розбіжність.

$$15.1. \text{ а) } \int_0^{\infty} \frac{xdx}{16x^4+1};$$

$$15.2. \text{ а) } \int_1^{\infty} \frac{16xdx}{16x^4-1};$$

$$15.3. \text{ а) } \int_0^{\infty} \frac{x^3 dx}{\sqrt{16x^4+1}};$$

$$15.4. \text{ а) } \int_1^{\infty} \frac{xdx}{\sqrt{16x^4-1}};$$

$$15.5. \text{ а) } \int_{-\infty}^0 \frac{xdx}{\sqrt{(x^2+4)^3}};$$

$$\text{ б) } \int_0^1 \frac{dx}{\sqrt[3]{2-4x}}.$$

$$\text{ б) } \int_1^3 \frac{dx}{\sqrt{x^2-6x+9}}.$$

$$\text{ б) } \int_0^{1/3} \frac{e^{3+1/x}}{x^2} dx.$$

$$\text{ б) } \int_1^3 \frac{dx}{\sqrt[3]{(3-x)^5}}.$$

$$\text{ б) } \int_{1/3}^1 \frac{\ln(3x-1)}{3x-1} dx.$$

- 15.6. a) $\int_0^{\infty} \frac{x^2 dx}{\sqrt[3]{(x^3+8)^4}}$; б) $\int_{1/4}^1 \frac{dx}{20x^2-9x+1}$.
- 15.7. a) $\int_0^{\infty} \frac{xdx}{\sqrt[4]{(16+x^2)^5}}$; б) $\int_{1/2}^1 \frac{\ln 2dx}{(1-x)\ln^2(1-x)}$.
- 15.8. a) $\int_4^{\infty} \frac{xdx}{\sqrt{x^2-4x+1}}$; б) $\int_0^{2/3} \frac{\sqrt[3]{\ln(2-3x)}}{2-3x} dx$.
- 15.9. a) $\int_{-1}^{\infty} \frac{dx}{\pi(x^2+4x+5)}$; б) $\int_0^1 \frac{xdx}{1-x^4}$.
- 15.10. a) $\int_{-1}^{\infty} \frac{xdx}{x^2+4x+5}$; б) $\int_0^{\pi/6} \frac{\cos 3x}{\sqrt[6]{(1-\sin 3x)^5}} dx$.
- 15.11. a) $\int_0^{\infty} \frac{\operatorname{arctg} 2x}{\pi(1+4x^2)} dx$; б) $\int_0^1 \frac{2xdx}{\sqrt{1-x^4}}$.
- 15.12. a) $\int_{1/2}^{\infty} \frac{16dx}{\pi(4x^2+4x+5)}$; б) $\int_{-1/3}^0 \frac{dx}{\sqrt[3]{1+3x}}$.
- 15.13. a) $\int_0^{\infty} \frac{xdx}{4x^2+4x+5}$; б) $\int_{3/4}^1 \frac{dx}{\sqrt[5]{3-4x}}$.
- 15.14. a) $\int_0^{\infty} \frac{(x+2)dx}{\sqrt[3]{(x^2+4x+1)^4}}$; б) $\int_0^{\pi/2} \frac{e^{\operatorname{tg} x}}{\cos^2 x} dx$.
- 15.15. a) $\int_0^{\infty} \frac{3-x^2}{x^2+4} dx$; б) $\int_0^1 \frac{2e^{1-\frac{2}{\pi}\arcsin x}}{\pi\sqrt{1-x^2}} dx$.
- 15.16. a) $\int_0^{\infty} \frac{x^2 dx}{\sqrt[3]{(x^3+8)^4}}$; б) $\int_1^2 \frac{dx}{\sqrt[5]{4x-x^2-4}}$.
- 15.17. a) $\int_0^{\infty} \frac{xdx}{\sqrt[4]{(16+x^2)^5}}$; б) $\int_{\pi/2}^{\pi} \frac{\sin x dx}{\sqrt[7]{\cos^2 x}}$.
- 15.18. a) $\int_0^{\infty} \sqrt{\frac{2}{\pi}} \frac{\sqrt{\operatorname{arctg} 2x}}{1+4x^2} dx$; б) $\int_{-3/4}^0 \frac{dx}{\sqrt{4x+3}}$.
- 15.19. a) $\int_1^{\infty} \frac{4dx}{x(1+\ln^2 x)}$; б) $\int_1^2 \frac{xdx}{\sqrt{(x^2-1)^3 \ln 2}}$.

- 15.20. a) $\int_0^{\infty} x \sin x dx$; б) $\int_0^{1/3} \frac{dx}{9x^2 - 9x + 2}$.
- 15.21. a) $\int_{-\infty}^{-1} \frac{7dx}{(x^2 - 4x) \ln 5}$; б) $\int_0^{\pi/2} \frac{3 \sin^3 x dx}{\sqrt{\cos x}}$.
- 15.22. a) $\int_{1/3}^{\infty} \frac{\pi dx}{(1 + 9x^2) \operatorname{arctg}^2 3x}$; б) $\int_0^3 \frac{\sqrt[3]{9} x dx}{\sqrt[3]{9 - x^2}}$.
- 15.23. a) $\int_2^{\infty} \frac{dx}{(4 + x^2) \sqrt{\pi \operatorname{arctg} \frac{x}{2}}}$; б) $\int_0^1 \frac{x^4 dx}{\sqrt[3]{1 - x^5}}$.
- 15.24. a) $\int_1^{\infty} \frac{dx}{(x^2 + 2x) \ln 3}$; б) $\int_0^2 \frac{x^2 dx}{\sqrt{64 - x^6}}$.
- 15.25. a) $\int_0^{\infty} e^{-3x} x dx$; б) $\int_{1/2}^1 \frac{dx}{\sqrt{1 - 2x}}$.
- 15.26. a) $\int_{-\infty}^0 \left(\frac{x^2}{x^3 - 1} - \frac{x}{1 + x^2} \right) dx$; б) $\int_1^5 \frac{x^2 dx}{\sqrt{31(x^2 - 1)}}$.
- 15.27. a) $\int_0^{\infty} \frac{dx}{2x^2 - 2x + 1}$; б) $\int_1^{3/2} \frac{dx}{\sqrt{3x - x^2 - 2}}$.
- 15.28. a) $\int_1^{\infty} \frac{dx}{x^2(x+1)}$; б) $\int_0^4 \frac{10x dx}{\sqrt[4]{(16 - x^2)^3}}$.
- 15.29. a) $\int_{e^2}^{\infty} \frac{dx}{x(\ln x - 1)^2}$; б) $\int_0^{1/4} \frac{dx}{\sqrt[3]{1 - 4x}}$.
- 15.30. a) $\int_1^{\infty} \frac{10x dx}{(6x^2 - 5x + 1) \ln \frac{3}{4}}$; б) $\int_0^{1/2} \frac{dx}{(2x - 1)^2}$.