

Завдання 1. Обчислити інтеграли.

$$1.1. \int \frac{3\sqrt[3]{x^2} - 2x}{\sqrt{x}} dx .$$

$$1.3. \int \frac{3\sqrt{x} + 4x^2 - 5}{2x} dx .$$

$$1.5. \int \frac{\sqrt[4]{x} - 2x + 5}{x^2} dx .$$

$$1.7. \int (\sqrt[3]{x} - \frac{2\sqrt[4]{x}}{x} + 3) dx .$$

$$1.9. \int \frac{3x^2 - \sqrt[5]{x} + 2}{x} dx .$$

$$1.11. \int \frac{\sqrt[6]{x^5} - 5x^2 + 3}{x} dx .$$

$$1.13. \int (x^2 - \frac{\sqrt[6]{x}}{x} - 3) dx .$$

$$1.15. \int (\frac{\sqrt[3]{x}}{x} + 2x^3 - 4) dx .$$

$$1.17. \int (2x^3 - 3\sqrt{x^5} + \frac{4}{x}) dx .$$

$$1.19. \int \frac{3x^2 - \sqrt{x^2} + 7}{x^2} dx .$$

$$1.21. \int (\sqrt[5]{x^2} - \frac{2}{x^3} + 4) dx .$$

$$1.23. \int \frac{\sqrt[3]{x} - 2x^3 + 4}{x^2} dx .$$

$$1.25. \int (\sqrt[5]{x} - \frac{4}{x^5} + 2) dx .$$

$$1.27. \int (\frac{\sqrt[3]{x}}{x} - \frac{2}{x^3} + 1) dx .$$

$$1.29. \int (\frac{\sqrt[3]{x^2}}{x} - \frac{7}{x^3} + 5) dx .$$

$$1.2. \int \frac{2x^2 + 3\sqrt{x} - 1}{2x} dx .$$

$$1.4. \int \frac{2\sqrt{x} - x^2 + 3}{\sqrt[3]{x}} dx .$$

$$1.6. \int \frac{2x^3 - \sqrt{x} + 4}{\sqrt{x}} dx .$$

$$1.8. \int \frac{2x^3 - \sqrt{x^5} + 1}{\sqrt{x}} dx .$$

$$1.10. \int \frac{2x^3 - \sqrt{x} + 4}{x^2} dx .$$

$$1.12. \int (x\sqrt{x} - \frac{1}{\sqrt{x^3}} + 1) dx .$$

$$1.14. \int \frac{\sqrt[3]{x^2} - 2x^5 + 3}{x} dx .$$

$$1.16. \int \frac{\sqrt{x^3} - 3x^4 + 2}{x} dx .$$

$$1.18. \int \frac{2x^3 - \sqrt{x^5} + 5}{x^2} dx .$$

$$1.20. \int \frac{3x^4 - \sqrt[3]{x^2} + 1}{x^2} dx .$$

$$1.22. \int \frac{\sqrt{x} - 2x^3 + 6}{x} dx .$$

$$1.24. \int (\sqrt{x} - \frac{3x^2}{\sqrt{x^3}} + 2) dx .$$

$$1.26. \int \frac{\sqrt[7]{x^6} - 2x^2 + 3}{x} dx .$$

$$1.28. \int (\frac{2x^2}{\sqrt{x}} - \frac{5}{x} + 6) dx .$$

$$1.30. \int (\frac{5x^2}{\sqrt{x}} - \sqrt[3]{x^2} + 2) dx .$$

Завдання 2. Обчислити інтеграли.

$$2.1. \int \sqrt{3+x} dx .$$

$$2.2. \int \sqrt[3]{1+x} dx .$$

$$2.3. \int \sqrt[3]{(1+x)^2} dx .$$

$$2.4. \int \frac{dx}{\sqrt[3]{1+x}} .$$

$$2.5. \int \frac{dx}{\sqrt[3]{(1-x)^3}} .$$

$$2.6. \int \frac{dx}{\sqrt[3]{2+x}} .$$

$$2.7. \int (1-4x)^7 dx .$$

$$2.8. \int (1+4x)^5 dx .$$

$$2.9. \int (1-3x)^4 dx .$$

$$2.10. \int \sqrt{1+3x} dx .$$

$$2.11. \int \sqrt{5-4x} dx .$$

$$2.12. \int \frac{dx}{\sqrt[3]{5+3x}} .$$

$$2.13. \int \frac{dx}{\sqrt[3]{(1-4x)^5}} .$$

$$2.14. \int \frac{dx}{\sqrt[3]{(3-4x)^2}} .$$

$$2.15. \int \frac{dx}{\sqrt[3]{2-5x}} .$$

$$2.16. \int \sqrt[5]{3-2x} dx .$$

$$2.17. \int \sqrt[4]{1+3x} dx .$$

$$2.18. \int \sqrt[3]{1+3x} dx .$$

$$2.19. \int \frac{dx}{\sqrt[3]{(3-x)^5}} .$$

$$2.20. \int \frac{dx}{\sqrt[3]{3+x}} .$$

$$2.21. \int \frac{dx}{(2+x)^3} .$$

$$2.22. \int \sqrt[3]{5-2x} dx .$$

$$2.23. \int \sqrt{5-4x} dx .$$

$$2.24. \int \sqrt[5]{(6-5x)^2} dx .$$

$$2.25. \int \sqrt[4]{2-5x} dx .$$

$$2.26. \int \sqrt[3]{4-2x} dx .$$

$$2.27. \int \sqrt{3-4x} dx .$$

$$2.28. \int \sqrt[5]{3+2x} dx .$$

$$2.29. \int \sqrt[4]{(3+5x)^3} dx .$$

$$2.30. \int \sqrt[3]{(2-x)^2} dx .$$

Завдання 3. Обчислити інтеграли.

$$3.1. \int \frac{\sqrt{3}dx}{9x^2-3} .$$

$$3.2. \int \frac{dx}{\sqrt{9x^2+3}} .$$

$$3.3. \int \frac{dx}{9x^2+3}.$$

$$3.5. \int \frac{dx}{\sqrt{3-9x^2}}.$$

$$3.7. \int \frac{3dx}{\sqrt{7x^2-4}}.$$

$$3.9. \int \frac{dx}{5x^2-3}.$$

$$3.11. \int \frac{dx}{\sqrt{5x^2+3}}.$$

$$3.13. \int \frac{\sqrt{5}dx}{\sqrt{3-4x^2}}.$$

$$3.15. \int \frac{dx}{2x^2+7}.$$

$$3.17. \int \frac{x dx}{\sqrt{5-4x^2}}.$$

$$3.19. \int \frac{3x dx}{4x^2+1}.$$

$$3.21. \int \frac{dx}{\sqrt{2-5x^2}}.$$

$$3.23. \int \frac{dx}{\sqrt{7x^2-3}}.$$

$$3.25. \int \frac{dx}{2x^2+3}.$$

$$3.27. \int \frac{dx}{2x^2+9}.$$

$$3.29. \int \frac{dx}{\sqrt{9x^2+2}}.$$

$$3.4. \int \frac{9dx}{\sqrt{9x^2-3}}.$$

$$3.6. \int \frac{dx}{7x^2-4}.$$

$$3.8. \int \frac{dx}{5x^2+3}.$$

$$3.10. \int \frac{dx}{\sqrt{3-5x^2}}.$$

$$3.12. \int \frac{dx}{\sqrt{4-7x^2}}.$$

$$3.14. \int \frac{dx}{\sqrt{2x^2-9}}.$$

$$3.16. \int \frac{dx}{\sqrt{3x^2+1}}.$$

$$3.18. \int \frac{x dx}{\sqrt{5-3x^2}}.$$

$$3.20. \int \frac{4x dx}{\sqrt{3-4x^2}}.$$

$$3.22. \int \frac{dx}{2x^2-5}.$$

$$3.24. \int \frac{dx}{5x^2+2}.$$

$$3.26. \int \frac{dx}{\sqrt{5x^2+1}}.$$

$$3.28. \int \frac{dx}{\sqrt{9-2x^2}}.$$

$$3.30. \int \frac{dx}{5x^2-4}.$$

Завдання 4. Обчислити інтеграли.

$$4.1. \int \frac{dx}{(2x+1)\sqrt[3]{\ln^2(2x+1)}}.$$

$$4.2. \int \frac{\sqrt[3]{\ln^2(1-x)}}{x-1} dx.$$

$$4.3. \int \frac{dx}{(1-x)\sqrt[3]{\ln^2(1-x)}}.$$

$$4.5. \int \frac{\ln^3(1-x)}{x-1} dx.$$

$$4.7. \int \frac{\sqrt[3]{\ln(3x+1)}}{3x+1} dx.$$

$$4.9. \int \frac{dx}{(x+1)\sqrt[3]{\ln(x+1)}}.$$

$$4.11. \int \frac{\sqrt{\ln^5(x+1)}}{x+1} dx.$$

$$4.13. \int \frac{\sqrt{\ln^3(x+1)}}{x+1} dx.$$

$$4.15. \int \frac{dx}{(x+1)^5\sqrt{\ln(x+1)}}.$$

$$4.17. \int \frac{\sqrt{\ln^3(x+1)}}{x+1} dx.$$

$$4.19. \int \frac{\sqrt{\ln^5(x+1)}}{x+1} dx.$$

$$4.21. \int \frac{dx}{(x+1)\sqrt[3]{\ln(x+1)}}.$$

$$4.23. \int \frac{\sqrt{\ln^3(x+3)}}{x+3} dx.$$

$$4.25. \int \frac{\sqrt{\ln^3(x+3)}}{x+3} dx.$$

$$4.27. \int \frac{\ln(3x+5)}{3x+5} dx.$$

$$4.29. \int \frac{\ln^6(x+9)}{x+9} dx.$$

$$4.4. \int \frac{dx}{(1-x)\sqrt{\ln^3(1-x)}}.$$

$$4.6. \int \frac{\sqrt{\ln(2x-1)}}{2x-1} dx.$$

$$4.8. \int \frac{dx}{(x+1)\ln^2(x+1)}.$$

$$4.10. \int \frac{dx}{(x+1)\ln^2(x+1)}.$$

$$4.12. \int \frac{\sqrt[7]{\ln^2(x+1)}}{x+1} dx.$$

$$4.14. \int \frac{dx}{(x+1)\sqrt[3]{\ln(x+1)}}.$$

$$4.16. \int \frac{dx}{(x+2)\sqrt{\ln(x+2)}}.$$

$$4.18. \int \frac{dx}{(x-3)\ln^4(x-3)}.$$

$$4.20. \int \frac{\ln^3(x-5)}{x-5} dx.$$

$$4.22. \int \frac{dx}{(x-3)\ln^4(x-3)}.$$

$$4.24. \int \frac{\sqrt[3]{\ln^4(x-5)}}{x-5} dx.$$

$$4.26. \int \frac{\ln^5(x-8)}{x-8} dx.$$

$$4.28. \int \frac{dx}{(x-4)\ln^5(x-4)}.$$

$$4.30. \int \frac{\ln(3x+5)}{3x+5} dx.$$

Завдання 5. Обчислити інтеграли.

$$5.1. \int \frac{\sqrt[3]{\operatorname{arctg}^6 3x}}{1+9x^2} dx .$$

$$5.3. \int \frac{\arccos^2 3x}{\sqrt{1-9x^2}} dx .$$

$$5.5. \int \frac{\sqrt[3]{\arccos^2 x}}{\sqrt{1-x^2}} dx .$$

$$5.7. \int \frac{\arccos^3 2x}{\sqrt{1-4x^2}} dx .$$

$$5.9. \int \frac{\arcsin^5 2x}{\sqrt{1-4x^2}} dx .$$

$$5.11. \int \frac{\arccos^3 2x}{\sqrt{1-4x^2}} dx .$$

$$5.13. \int \frac{\arccos 4x}{\sqrt{1-16x^2}} dx .$$

$$5.15. \int \frac{\arcsin^3 2x}{\sqrt{1-4x^2}} dx .$$

$$5.17. \int \frac{\sqrt[3]{\operatorname{arctg} 2x}}{1+4x^2} dx .$$

$$5.19. \int \frac{\sqrt[3]{\operatorname{arctg}^3 x}}{1+x^2} dx .$$

$$5.21. \int \frac{dx}{(1+x^2)\operatorname{arctg}^5 x} .$$

$$5.23. \int \frac{\sqrt[3]{\arccos 2x}}{\sqrt{1-4x^2}} dx .$$

$$5.25. \int \frac{\arcsin^2 5x}{\sqrt{1-25x^2}} dx .$$

$$5.27. \int \frac{\operatorname{arctg}^8 3x}{1+9x^2} dx .$$

$$5.29. \int \frac{\sqrt[5]{\operatorname{arctg}^3 x}}{1+x^2} dx .$$

$$5.2. \int \frac{\sqrt[3]{\arcsin x}}{\sqrt{1-x^2}} dx .$$

$$5.4. \int \frac{\operatorname{arcctg}^3 2x}{1+4x^2} dx .$$

$$5.6. \int \frac{dx}{(1+x^2)\operatorname{arctg}^3 x} .$$

$$5.8. \int \frac{\sqrt[3]{\operatorname{arctg}^2 x}}{1+x^2} dx .$$

$$5.10. \int \frac{dx}{\sqrt{1-x^2} \arcsin^4 x} .$$

$$5.12. \int \frac{\operatorname{arcctg}^7 3x}{1+9x^2} dx .$$

$$5.14. \int \frac{\arcsin^4 x}{\sqrt{1-x^2}} dx .$$

$$5.16. \int \frac{dx}{(1+x^2)\operatorname{arctg}^7 x} .$$

$$5.18. \int \frac{\arccos^6 3x}{\sqrt{1-9x^2}} dx .$$

$$5.20. \int \frac{dx}{(1+x^2)\sqrt{\operatorname{arctg} x}} .$$

$$5.22. \int \frac{\arccos^7 x dx}{\sqrt{1-x^2}} .$$

$$5.24. \int \frac{\operatorname{arcctg}^4 5x}{1+25x^2} dx .$$

$$5.26. \int \frac{dx}{\sqrt{1-25x^2} \arcsin 5x} .$$

$$5.28. \int \frac{\arccos^2 7x}{\sqrt{1-49x^2}} dx .$$

$$5.30. \int \frac{\operatorname{arcctg}^4 8x}{1+64x^2} dx .$$

Завдання 6. Обчислити інтеграли.

$$\mathbf{6.1.} \int \frac{dx}{4x^2 - 5x + 4}.$$

$$\mathbf{6.3.} \int \frac{dx}{2x^2 - 7x + 1}.$$

$$\mathbf{6.5.} \int \frac{dx}{5x^2 + 2x + 7}.$$

$$\mathbf{6.7.} \int \frac{dx}{2x^2 - 11x + 2}.$$

$$\mathbf{6.9.} \int \frac{dx}{3x^2 - 12x + 3}.$$

$$\mathbf{6.11.} \int \frac{dx}{x^2 - 5x + 6}.$$

$$\mathbf{6.13.} \int \frac{dx}{3x^2 - 8x - 3}.$$

$$\mathbf{6.15.} \int \frac{dx}{5x - x^2 - 6}.$$

$$\mathbf{6.17.} \int \frac{dx}{\sqrt{3x^2 - 4x + 1}}.$$

$$\mathbf{6.19.} \int \frac{dx}{\sqrt{x^2 + 6x + 8}}.$$

$$\mathbf{6.21.} \int \frac{dx}{\sqrt{3 + 2x - 2x^2}}.$$

$$\mathbf{6.23.} \int \frac{dx}{\sqrt{1 + x - x^2}}.$$

$$\mathbf{6.25.} \int \frac{dx}{\sqrt{2x + 3 - x^2}}.$$

$$\mathbf{6.27.} \int \frac{dx}{\sqrt{1 + 2x - x^2}}.$$

$$\mathbf{6.29.} \int \frac{dx}{\sqrt{2 + 4x - 3x^2}}.$$

$$\mathbf{6.2.} \int \frac{dx}{x^2 - 4x + 10}.$$

$$\mathbf{6.4.} \int \frac{dx}{2x^2 + x - 6}.$$

$$\mathbf{6.6.} \int \frac{dx}{2x^2 - 2x + 1}.$$

$$\mathbf{6.8.} \int \frac{dx}{2x^2 + x + 2}.$$

$$\mathbf{6.10.} \int \frac{dx}{2x^2 + 3x + 2}.$$

$$\mathbf{6.12.} \int \frac{dx}{2x - 3 - 4x^2}.$$

$$\mathbf{6.14.} \int \frac{dx}{8 - 2x - x^2}.$$

$$\mathbf{6.16.} \int \frac{dx}{\sqrt{4 + 8x - x^2}}.$$

$$\mathbf{6.18.} \int \frac{dx}{\sqrt{2 - 3x - 2x^2}}.$$

$$\mathbf{6.20.} \int \frac{dx}{\sqrt{2 + 8x - 2x^2}}.$$

$$\mathbf{6.22.} \int \frac{dx}{2 - 2x - 3x^2}.$$

$$\mathbf{6.24.} \int \frac{dx}{\sqrt{5x^2 - 10x + 4}}.$$

$$\mathbf{6.26.} \int \frac{dx}{4x^2 - 8x + 3}.$$

$$\mathbf{6.28.} \int \frac{dx}{\sqrt{4x^2 - x + 4}}.$$

$$\mathbf{6.30.} \int \frac{dx}{4x^2 + 2x + 4}.$$

Завдання 7. Обчислити інтеграли.

$$7.1. \int \frac{x+1}{2x^2+3x-4} dx .$$

$$7.2. \int \frac{x+6}{3x^2+x+1} dx .$$

$$7.3. \int \frac{2x-1}{3x^2-2x+6} dx .$$

$$7.4. \int \frac{xdx}{2x^2+x+5} dx .$$

$$7.5. \int \frac{x+5}{x^2+x-2} dx .$$

$$7.6. \int \frac{3x-2}{5x^2-3x+2} dx .$$

$$7.7. \int \frac{x+4}{2x^2-6x-8} dx .$$

$$7.8. \int \frac{x+4}{2x^2-7x+1} dx .$$

$$7.9. \int \frac{5x-2}{2x^2-5x+2} dx .$$

$$7.10. \int \frac{4x-1}{4x^2-4x+5} dx .$$

$$7.11. \int \frac{x+1}{2x^2+x+1} dx .$$

$$7.12. \int \frac{x+1}{3x^2-2x-3} dx .$$

$$7.13. \int \frac{4x+8}{4x^2+6x-13} dx .$$

$$7.14. \int \frac{5x+1}{x^2-4x+1} dx .$$

$$7.15. \int \frac{xdx}{2x^2+2x+5} dx .$$

$$7.16. \int \frac{2x-13}{\sqrt{3x^2-3x-16}} dx .$$

$$7.17. \int \frac{x-3}{\sqrt{2x^2-4x-1}} dx .$$

$$7.18. \int \frac{x-1}{\sqrt{3x^2-x+5}} dx .$$

$$7.19. \int \frac{2x+1}{\sqrt{1+x-3x^2}} dx .$$

$$7.20. \int \frac{2x+5}{\sqrt{4x^2+8x+9}} dx .$$

$$7.21. \int \frac{2x-10}{\sqrt{1+x-x^2}} dx .$$

$$7.22. \int \frac{2x-8}{\sqrt{1-x+x^2}} dx .$$

$$7.23. \int \frac{3x+4}{\sqrt{x^2+6x+13}} dx .$$

$$7.24. \int \frac{3x-1}{\sqrt{2x^2-5x+1}} dx .$$

$$7.25. \int \frac{5x+2}{\sqrt{x^2+3x-4}} dx .$$

$$7.26. \int \frac{x-4}{\sqrt{2x^2-x+7}} dx .$$

$$7.27. \int \frac{2x-1}{\sqrt{x^2-3x+4}} dx .$$

$$7.28. \int \frac{4x+1}{\sqrt{2+x-x^2}} dx .$$

$$7.29. \int \frac{5x-3}{\sqrt{2x^2+4x-5}} dx .$$

$$7.30. \int \frac{3x+2}{\sqrt{4+2x-x^2}} dx .$$

Завдання 8. Обчислити інтеграли.

$$8.1. \int (x-7) \cos 2x dx .$$

$$8.3. \int (x-5) \cos x dx .$$

$$8.5. \int (x+8) \sin 3x dx .$$

$$8.7. \int (x+4) \cos \frac{x}{2} dx .$$

$$8.9. \int \ln(x-5) dx .$$

$$8.11. \int x^2 e^{-x} dx .$$

$$8.13. \int \arcsin 5x dx .$$

$$8.15. \int x^2 e^{3x} dx .$$

$$8.17. \int \arcsin 2x dx .$$

$$8.19. \int x e^{-4x} dx .$$

$$8.21. \int x \sin(x-2) dx .$$

$$8.23. \int x \sin(x-5) dx .$$

$$8.25. \int \operatorname{arctg} \frac{x}{2} dx .$$

$$8.27. \int \ln(2x-1) dx .$$

$$8.29. \int \operatorname{arctg} \frac{x}{4} dx .$$

$$8.2. \int (x-4) \sin 2x dx .$$

$$8.4. \int (x-4) \cos 2x dx .$$

$$8.6. \int (x+2) \sin \frac{x}{2} dx .$$

$$8.8. \int (x-9) \sin \frac{x}{2} dx .$$

$$8.10. \int \operatorname{arctg} 2x dx .$$

$$8.12. \int \operatorname{arctg} 4x dx .$$

$$8.14. \int x \operatorname{arctg} x dx .$$

$$8.16. \int x \cos(x+4) dx .$$

$$8.18. \int (x^2 - 3) e^x dx .$$

$$8.20. \int \arcsin 3x dx .$$

$$8.22. \int x \cos(x+4) dx .$$

$$8.24. \int x \cos(x+6) dx .$$

$$8.26. \int \ln(x+8) dx .$$

$$8.28. \int \arccos \frac{x}{5} dx .$$

$$8.30. \int \arccos \frac{x}{3} dx .$$

Завдання 9. Обчислити інтеграли.

$$9.1. \int \frac{dx}{2 + \sqrt{x+3}} .$$

$$9.2. \int \frac{x dx}{\sqrt{x+3}} .$$

$$9.3. \int \frac{x^2 dx}{\sqrt{x-3}} .$$

$$9.4. \int \frac{x dx}{2 + \sqrt{x+4}} .$$

$$9.5. \int \frac{x^3 dx}{\sqrt{x+1}} .$$

$$9.6. \int \frac{x+1}{x \sqrt{x+2}} dx .$$

$$9.7. \int \frac{dx}{(x+1)\sqrt{x+4}} .$$

$$9.8. \int \frac{\sqrt{x+2}}{x-3} dx .$$

$$9.9. \int \frac{dx}{\sqrt{x+3}}.$$

$$9.11. \int \frac{1+x}{x+\sqrt{x}} dx.$$

$$9.13. \int \frac{\sqrt{x}dx}{x-1}.$$

$$9.15. \int \frac{dx}{1+\sqrt{x-1}}.$$

$$9.17. \int \frac{x+1}{x\sqrt{x-1}} dx.$$

$$9.19. \int \frac{x^2dx}{\sqrt{x-4}}.$$

$$9.21. \int \frac{x^3dx}{\sqrt{x+2}}.$$

$$9.23. \int \frac{dx}{\sqrt{x(x-1)}}.$$

$$9.25. \int \frac{dx}{x\sqrt{x-2}}.$$

$$9.27. \int \frac{x-1}{x\sqrt{x-2}} dx.$$

$$9.29. \int \frac{dx}{3+\sqrt{x-6}}.$$

$$9.10. \int \frac{dx}{\sqrt{x(x+3)}}.$$

$$9.12. \int \frac{xdx}{\sqrt{x-1}}.$$

$$9.14. \int \frac{dx}{3+\sqrt{x+5}}.$$

$$9.16. \int \frac{dx}{x\sqrt{x-7}}.$$

$$9.18. \int \frac{x^3dx}{\sqrt{x-7}}.$$

$$9.20. \int \frac{\sqrt{x+4}}{x} dx.$$

$$9.22. \int \frac{\sqrt{x}dx}{x+10}.$$

$$9.24. \int \frac{dx}{1+\sqrt{x-2}}.$$

$$9.26. \int \frac{x^2dx}{\sqrt{x-2}}.$$

$$9.28. \int \frac{x^3dx}{\sqrt{x+6}}.$$

$$9.30. \int \frac{dx}{2+\sqrt{x-8}}.$$

Завдання 10. Обчислити інтеграли.

$$10.1. \int \cos^4 3x \sin^2 3x dx.$$

$$10.2. \int \sqrt[5]{\sin^4 x} \cos^3 3x dx.$$

$$10.3. \int \cos^3 x \sin^8 x dx.$$

$$10.4. \int \cos^4 x \sin^3 x dx.$$

$$10.5. \int \frac{\cos^3 x dx}{\sqrt[3]{\sin^4 x}}.$$

$$10.6. \int \sqrt[5]{\sin^3 2x} \cos^3 2x dx.$$

$$10.7. \int \frac{\cos^3 x}{\sqrt[3]{\sin^2 x}} dx.$$

$$10.8. \int \frac{\sin^3 x}{\sqrt[3]{\cos^4 x}} dx.$$

$$10.9. \int \frac{3 \sin^3 x}{\cos^4 x} dx.$$

$$10.10. \int \sin^5 x \cos^4 x dx.$$

$$10.11. \int \frac{\sin^3 x}{\sqrt[5]{\cos^3 x}} dx .$$

$$10.13. \int \sqrt[3]{\sin^2 x} \cos^3 x dx .$$

$$10.15. \int \frac{\cos^3 x dx}{\sqrt[5]{\sin^3 x}} .$$

$$10.17. \int \frac{\sin^3 x}{\sqrt[3]{\cos^2 x}} dx .$$

$$10.19. \int \sin^4 2x \cos^2 2x dx .$$

$$10.21. \int \frac{\sin^3 2x}{\sqrt[3]{\cos^2 2x}} dx .$$

$$10.23. \int \sin^2 x \cos^4 x dx .$$

$$10.25. \int \sin^3 x \cos^8 x dx .$$

$$10.27. \int \sin^5 x \sqrt[5]{\cos^3 x} dx .$$

$$10.29. \int \sin^4 3x \cos^2 3x dx .$$

$$10.12. \int \sqrt[3]{\cos^2 x} \sin^3 x dx .$$

$$10.14. \int \sqrt[5]{\cos^3 2x} \sin^3 2x dx .$$

$$10.16. \int \sin^2 2x \cos^4 2x dx .$$

$$10.18. \int \sqrt[3]{\cos^4 x} \sin^3 x dx .$$

$$10.20. \int \frac{\cos^3 2x}{\sqrt[3]{\sin^2 2x}} dx .$$

$$10.22. \int \sin^4 x \cos^3 x dx .$$

$$10.24. \int \sin^4 x \cos^2 x dx .$$

$$10.26. \int \frac{3 \cos^3 x}{\sin^4 x} dx .$$

$$10.28. \int \sin^4 x \cos^5 x dx .$$

$$10.30. \int \frac{\sin^3 x}{\sqrt[3]{\cos^4 x}} dx .$$

Завдання 11. Користуючись обчислити інтеграли.

$$11.1. \int_0^{\sqrt[3]{3}} x^2 \sqrt[3]{1+x^2} dx .$$

$$11.3. \int_0^1 \frac{x^2 dx}{x^2 + 1} .$$

$$11.5. \int_0^{\pi/2} \frac{\cos x}{1+\cos x} dx .$$

$$11.7. \int_0^{-3} \frac{dx}{\sqrt{25+3x}} .$$

$$11.9. \int_1^e \frac{1+\ln x}{x} dx .$$

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$$11.2. \int_0^{12\sqrt{3}} \frac{12x^5 dx}{\sqrt{x^6+1}} .$$

$$11.4. \int_0^{\frac{\pi}{2}} \sin x \cos^2 x dx .$$

$$11.6. \int_{3/4}^{4/3} \frac{dx}{x^2+1} .$$

$$11.8. \int_0^2 \frac{x^3 dx}{\sqrt{x^4+4}} .$$

$$11.10. \int_0^1 \frac{x^3}{x^8+1} dx .$$

$$11.11. \int_{\pi/4}^{\pi/2} \frac{dx}{1-\cos^2 x}.$$

$$11.13. \int_0^1 x^3 \sqrt{4+5x^4} dx.$$

$$11.15. \int_1^2 \frac{e^{1/x}}{x^2} dx.$$

$$11.17. \int_0^1 3(x^2 + x^2 e^{x^3}) dx.$$

$$11.19. \int_1^{\sqrt{3}} \frac{x^2 dx}{1+x^6}.$$

$$11.21. \int_1^{\sqrt{e}} \frac{dx}{x\sqrt{1-\ln^2 x}}.$$

$$11.23. \int_{\pi/6}^{\pi/2} \sin x \cos^3 x dx.$$

$$11.25. \int_0^1 \frac{dx}{\sqrt{4-3x}}.$$

$$11.27. \int_1^e \frac{\ln^2 x}{x} dx.$$

$$11.29. \int_{\pi/6}^{\pi/2} \cos \alpha \sin^3 \alpha d\alpha.$$

$$11.12. \int_2^5 \frac{dx}{\sqrt{5+4x-x^2}}.$$

$$11.14. \int_{-\pi}^{\pi} \sin^2 \frac{x}{2} dx.$$

$$11.16. \int_0^{1/2} \frac{x dx}{\sqrt{1-x^2}}.$$

$$11.18. \int_{\pi^2/9}^{\pi^2} \frac{\cos \sqrt{x}}{\sqrt{x}} dx.$$

$$11.20. \int_1^e \frac{\sin \ln x}{x} dx.$$

$$11.22. \int_3^8 \sqrt{x+1} dx.$$

$$11.24. \int_{\pi/18}^{\pi/6} 12 \operatorname{ctg} 3x dx.$$

$$11.26. \int_1^{\sqrt{2}} \frac{x dx}{\sqrt{4-x^2}}.$$

$$11.28. \int_{-1}^0 \frac{dx}{4x^2-9}.$$

$$11.30. \int_0^{\sqrt{\pi}/4} \frac{x dx}{\cos^2(x^2)}.$$

Завдання 12. Обчислити невласні інтеграли або довести їх розбіжність.

$$12.1. \text{a) } \int_0^\infty \frac{x dx}{16x^4+1};$$

$$12.2. \text{a) } \int_1^\infty \frac{16x dx}{16x^4-1};$$

$$12.3. \text{a) } \int_0^\infty \frac{x^3 dx}{\sqrt{16x^4+1}};$$

$$\text{б) } \int_0^1 \frac{dx}{\sqrt[3]{2-4x}}.$$

$$\text{б) } \int_1^3 \frac{dx}{\sqrt{x^2-6x+9}}.$$

$$\text{б) } \int_0^{1/3} \frac{e^{3+\frac{1}{x}}}{x^2} dx.$$

12.4. a) $\int_1^{\infty} \frac{xdx}{\sqrt[4]{16x^4 - 1}};$

6) $\int_1^3 \frac{dx}{\sqrt[3]{(3-x)^5}}.$

12.5. a) $\int_{-\infty}^0 \frac{xdx}{\sqrt{(x^2 + 4)^3}};$

6) $\int_{1/3}^1 \frac{\ln(3x-1)}{3x-1} dx.$

12.6. a) $\int_0^{\infty} \frac{x^2 dx}{\sqrt[3]{(x^3 + 8)^4}};$

6) $\int_{1/4}^1 \frac{dx}{20x^2 - 9x + 1}.$

12.7. a) $\int_0^{\infty} \frac{xdx}{\sqrt[4]{(16+x^2)^5}};$

6) $\int_{1/2}^1 \frac{\ln 2 dx}{(1-x)\ln^2(1-x)}.$

12.8. a) $\int_4^{\infty} \frac{xdx}{\sqrt{x^2 - 4x + 1}};$

6) $\int_0^{2/3} \frac{\sqrt[3]{\ln(2-3x)}}{2-3x} dx.$

12.9. a) $\int_{-1}^{\infty} \frac{dx}{\pi(x^2 + 4x + 5)};$

6) $\int_0^1 \frac{xdx}{1-x^4}.$

12.10. a) $\int_{-1}^{\infty} \frac{xdx}{x^2 + 4x + 5};$

6) $\int_0^{\pi/6} \frac{\cos 3x}{\sqrt[6]{(1-\sin 3x)^5}} dx.$

12.11. a) $\int_0^{\infty} \frac{\operatorname{arctg} 2x}{\pi(1+4x^2)} dx;$

6) $\int_0^1 \frac{2xdx}{\sqrt{1-x^4}}.$

12.12. a) $\int_{1/2}^{\infty} \frac{16dx}{\pi(4x^2 + 4x + 5)};$

6) $\int_{-1/3}^0 \frac{dx}{\sqrt[3]{1+3x}}.$

12.13. a) $\int_0^{\infty} \frac{xdx}{4x^2 + 4x + 5};$

6) $\int_{3/4}^1 \frac{dx}{\sqrt[3]{3-4x}}.$

12.14. a) $\int_0^{\infty} \frac{(x+2)dx}{\sqrt[3]{(x^2 + 4x + 1)^4}};$

6) $\int_0^{\pi/2} \frac{e^{\operatorname{tg} x}}{\cos^2 x} dx.$

12.15. a) $\int_0^{\infty} \frac{3-x^2}{x^2+4} dx;$

6) $\int_0^1 \frac{2e^{\frac{1-2\arcsin x}{\pi}}}{\pi\sqrt{1-x^2}} dx.$

12.16. a) $\int_0^{\infty} \frac{x^2 dx}{\sqrt[3]{(x^3 + 8)^4}};$

6) $\int_1^2 \frac{dx}{\sqrt[5]{4x - x^2 - 4}}.$

12.17. a) $\int_0^{\infty} \frac{xdx}{\sqrt[4]{(16+x^2)^5}};$

6) $\int_{\pi/2}^{\pi} \frac{\sin x dx}{\sqrt[7]{\cos^2 x}}.$

- 12.18.** a) $\int_0^{\infty} \sqrt{\frac{2}{\pi}} \frac{\sqrt{\arctg 2x}}{1+4x^2} dx$; 6) $\int_{-\sqrt[3]{4}}^0 \frac{dx}{\sqrt{4x+3}}$.
- 12.19.** a) $\int_1^{\infty} \frac{4dx}{x(1+\ln^2 x)}$; 6) $\int_1^2 \frac{x dx}{\sqrt{(x^2-1)^3 \ln 2}}$.
- 12.20.** a) $\int_0^{\infty} x \sin x dx$; 6) $\int_0^{1/3} \frac{dx}{9x^2-9x+2}$.
- 12.21.** a) $\int_{-\infty}^{-1} \frac{7dx}{(x^2-4x)\ln 5}$; 6) $\int_0^{\pi/2} \frac{3 \sin^3 x dx}{\sqrt{\cos x}}$.
- 12.22.** a) $\int_{1/3}^{\infty} \frac{\pi dx}{(1+9x^2) \operatorname{arctg}^2 3x}$; 6) $\int_0^3 \frac{\sqrt[3]{9} x dx}{\sqrt[3]{9-x^2}}$.
- 12.23.** a) $\int_2^{\infty} \frac{dx}{(4+x^2)\sqrt{\pi \operatorname{arctg} \frac{x}{2}}}$; 6) $\int_0^1 \frac{x^4 dx}{\sqrt[3]{1-x^5}}$.
- 12.24.** a) $\int_1^{\infty} \frac{dx}{(x^2+2x)\ln 3}$; 6) $\int_0^2 \frac{x^2 dx}{\sqrt{64-x^6}}$.
- 12.25.** a) $\int_0^{\infty} e^{-3x} x dx$; 6) $\int_{1/2}^1 \frac{dx}{\sqrt[9]{1-2x}}$.
- 12.26.** a) $\int_{-\infty}^0 \left(\frac{x^2}{x^3-1} - \frac{x}{1+x^2} \right) dx$; 6) $\int_1^5 \frac{x^2 dx}{\sqrt{31(x^2-1)}}$.
- 12.27.** a) $\int_0^{\infty} \frac{dx}{2x^2-2x+1}$; 6) $\int_1^{3/2} \frac{dx}{\sqrt{3x-x^2-2}}$.
- 12.28.** a) $\int_1^{\infty} \frac{dx}{x^2(x+1)}$; 6) $\int_0^4 \frac{10x dx}{\sqrt[4]{(16-x^2)^3}}$.
- 12.29.** a) $\int_{e^2}^{\infty} \frac{dx}{x(\ln x-1)^2}$; 6) $\int_0^{1/4} \frac{dx}{\sqrt[3]{1-4x}}$.
- 12.30.** a) $\int_1^{\infty} \frac{10x dx}{(6x^2-5x+1)\ln \frac{3}{4}}$; 6) $\int_0^{1/2} \frac{dx}{(2x-1)^2}$.

Завдання 13. Обчислити площину фігури, обмеженої заданими лініями.

- 13.1.** $y = x + 1$, $y = \cos x$, $y = 0$
- 13.2.** $y = x^2$, $y = 3 - x$.
- 13.3.** $y = \sqrt{x}$, $y = x^3$.
- 13.4.** $x = 7 \cos^3 t$, $y = 7 \sin^3 t$.
- 13.5.** $x^2 = 4y$, $y = 8/(x^2 + 4)$
- 13.6.** $xy = 6$, $x + y - 7 = 0$
- 13.7.** $y = 2^x$, $y = 2x - x^2$, $x = 0$, $x = 2$
- 13.8.** $y^2 = (4 - x^3)$, $x = 0$
- 13.9.** $y = x^3$, $y = 1$, $x = 0$
- 13.10.** $y^2 = x^3$, $x = 2$
- 13.11.** $y = x^2$, $y = 2 - x^2$
- 13.12.** $y^2 = 4x$, $x^2 = 4y$
- 13.13.** $y = 1/(1+x^2)$, $y = x^2/2$.
- 13.14.** $y^2 = x + 1$, $y^2 = 9 - x$.
- 13.15.** $y^2 = x^3$, $x = 0$, $y = 4$.

Завдання. Обчислити об'єм тіла, утвореного обертанням фігури Φ навколо вказаної осі координат.

- 13.16.** $\Phi: y = 2x - x^2$, $y = 0$, Ox .
- 13.17.** $\Phi: y^3 = x^2$, $y = 1$, Ox .
- 13.18.** $\Phi: y^2 = (x - 1)^3$, $x = 2$, Ox .
- 13.19.** $\Phi: \frac{x^2}{16} + \frac{y^2}{1} = 1$, Ox .
- 13.20.** $\Phi: x^3 = (y - 1)^2$, $x = 0$, $y = 0$, Ox .
- 13.21.** $\Phi: xy = 4$, $2x + y - 6 = 0$, Ox .
- 13.22.** $\Phi: y^2 = 4x/3$, $x = 3$, Ox .
- 13.23.** $\Phi: y = 2 - x^2$, $y = x^2$, Ox .
- 13.24.** $\Phi: y = -x^2 + 8$, $y = x^2$, Ox .
- 13.25.** $\Phi: y^2 = (x + 4)^3$, $x = 0$, Ox .
- 13.26.** $\Phi: y = \sin x$, $y = 0$, $(0 \leq x \leq \pi)$, Ox .
- 13.27.** $\Phi: y = e^x$, $x = 0$, $y = 0$, $x = 1$, Ox .
- 13.28.** $\Phi: 2y = x^2$, $2x + 2y - 3 = 0$, Ox .
- 13.29.** $\Phi: y = x - x^2$, $y = 0$, Ox .
- 13.30.** $\Phi: y^2 = 4x$, $x^2 = 4y$, Ox .